

# Conditional Exchange Rate Pass-Through: A DSGE Model Approach

Mariano J. Palleja

Rodrigo Gómez Award 2018

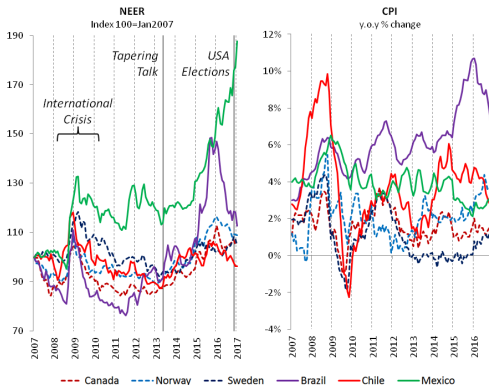
Apr 29, 2019

# Agenda

- 1 Introduction
- 2 Model and Estimation
  - Selection of Countries
  - Model
  - Parametrization
- 3 Conditional Pass-Through
  - Shocks Selection
  - Conditional Pass-Through Computation
- 4 Back in VAR
- 5 Conclusions
- 6 Appendices

# Motivation

Different inflationary responses when facing similar fluctuations in exchange rates



Source: Bruegel and International Financial Statistics - (IMF)

# Motivation

Usual approach to measure the transfer of the exchange rate to prices (ERPT): Reduced form equations.

Choudrhi and Hakura (2006)

$$\Delta P_t = \gamma_1 + \pi_1(L)\Delta P_{t-1} + \pi_2(L)\Delta S_t + \pi_3(L)\Delta P_{t-1}^* + \epsilon_t$$

$$ERPT = \sum_{\tau=0}^{T-1} \partial P_{t+\tau} / \partial S_t$$

- Weakness 1: Exchange rate movements assumed exogenous
- Weakness 2: Same coeff. independent of underlying shocks.

## Goal and Approach

- Goal: Are different ERPT due to different fundamentals or to different distribution of faced shocks?
- Approach:
  - 1) Estimate a DSGE model for two countries with an *a priori* different pass-through.
  - 2) Recover conditional ERPT coefficients.
  - 3) Analyze underlying shocks and compare their distribution.

# Agenda

- 1 Introduction
- 2 Model and Estimation
  - Selection of Countries
  - Model
  - Parametrization
- 3 Conditional Pass-Through
  - Shocks Selection
  - Conditional Pass-Through Computation
- 4 Back in VAR
- 5 Conclusions
- 6 Appendices

## Selection of Countries

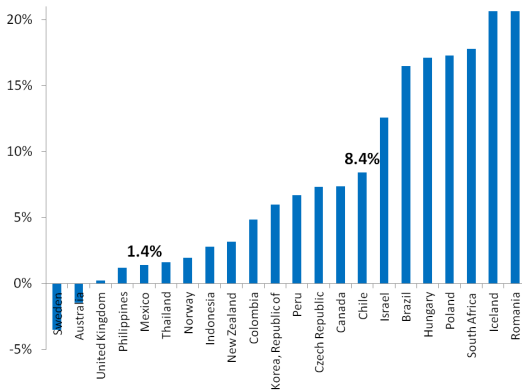
A Vector Autoregressive model (VAR) is estimated for 23 IT countries.

- Endogenous: GDP, NEER, CPI, and MPR.
- Exogenous: oil prices, Fed Fund Rate, and foreign CPI.
- Log. diff specification (interest rates included as p.p. differences).
- Optimal lag lengths are chosen as per the Schwarz-Bayesian and Hannan-Quinn information criterion.
- Quarterly data, period 2000q1-2016q2.
- Identification using Cholesky ordering: GDP, NEER, CPI, and MPR.
- $ERPT_{t_4} = (P_{t_4}^i - P_{t_0}^i) / (NEER_{t_4}^i - NEER_{t_0}^i)$ .

## Selection of Countries

### Nominal effective exchange rate pass through to CPI prices (4q).

Source: Own estimates based on IFS, Bruegel and Federal Reserve Bank of St. Louis.



**Chile and Mexico** are selected:  $\neq$  ERPT, data availability, similar features (EME, SOE, Comm Expo.)

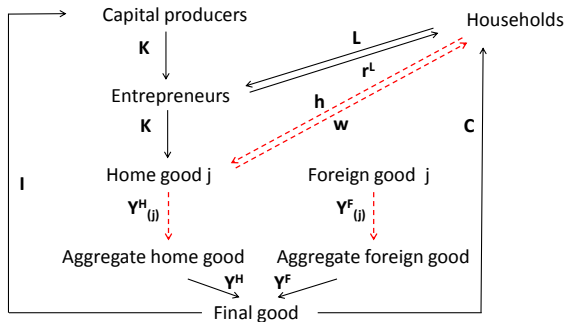


# Model

## García-Cicco, Justel and Kirchner (2014) - baseline

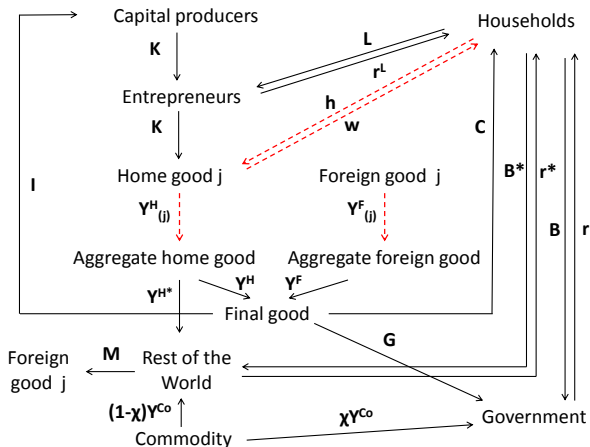
- SOE.
- Calvo pricing with indexation to  $(\pi_{t-1}$  and  $\pi^T)$  in
  - Home goods.
  - Imported goods (LCP).
  - Wages.
- Investment adjustment costs in capital production.
- Commodities sector.
- Monetary policy rule *a la* Taylor.
- 7 domestic shocks: preferences, investment efficiency, permanent technology shock, temporary technology shock, production of commodities, gov. expenditure and monetary policy rate.
- 6 external shocks: country premium, international interest rate, foreign inflation and foreign demand, commodities relative prices and UIP shocks.

# Model



Note: Dotted red lines indicate Calvo pricing/waging plus indexation to  $\pi_{t-1}$  and  $\pi^T$ .

# Model



Note: Dotted red lines indicate Calvo pricing/waging plus indexation to  $\pi_{t-1}$  and  $\pi^T$ .

## Model

- External debt rate

$$r_t^* = R_{t-1}^* \xi_{t-1} \varpi_{t-1} (\pi_t^*)^{-1}$$

- UIP

$$\widehat{R}_t = \widehat{R}_t^* + \widehat{\xi}_t + \mathbb{E}_t[\widehat{\pi}_{t+1}^S] + \widehat{\varpi}_t$$

where  $\xi_t$  is the Country Premium and  $\varpi_t$  are UIP shocks.

- Monetary Policy

$$\frac{R_t}{R_{SS}} = \left( \frac{R_{t-1}}{R_{SS}} \right)^{\rho R} \left[ \left( \frac{\pi_t}{\pi_{SS}} \right)^{\alpha_\pi} \left( \frac{Y_t/Y_{t-1}}{a_{t-1}} \right)^{\alpha_y} \right]^{1-\rho R} \exp(\varepsilon_t^R)$$

where  $\pi_{SS}$  is the inflation target and  $\varepsilon_t^R$  captures monetary policy shocks.

# Parametrization

- Calibration following previous papers and observable data.
- Parameters solved in steady state.
- Bayesian estimation.

**Same priors** were used for both countries.

## **14 observable variables.**

Nat. Accounts: GDP ( $Y$ ), investment ( $I$ ), consumption ( $C$ ) gov. expenditure ( $G$ ).

Prices: CPI inflation ( $\pi$ ), real wages ( $\pi^W$ ) main exported commodity price ( $p^{Co*}$ ).

Other domestic: commodity production ( $Y^{Co}$ ), monetary policy rate ( $R$ ), EMBI+Country ( $\xi$ ), nominal effective exchange rate ( $\pi^S$ ).

Foreign: LIBOR rate ( $R^*$ ), trading partners GDP ( $Y^*$ ) inflation ( $\pi^*$ ).

**Period**. Chile: 2001q3–2016q2, Mexico: 2003q1–2016q2.

# Parametrization

## Selected estimated parameters

| Param.       | Description                         | Prior |      | Posterior Mean |             |
|--------------|-------------------------------------|-------|------|----------------|-------------|
|              |                                     | Mean  | S.E. | Chile          | Mexico      |
| $\alpha^\pi$ | $\pi_t$ weight in MPR               | 1.5   | 0.1  | 1.49           | 1.55        |
| $\alpha^y$   | $y_t$ weight in MPR                 | 0.13  | 0.05 | 0.15           | 0.15        |
| $\rho^R$     | $R_{t-1}$ weight in MPR             | 0.75  | 0.1  | 0.84           | 0.8         |
| $\theta^H$   | Calvo prob. home good               | 0.75  | 0.1  | <u>0.50</u>    | <u>0.72</u> |
| $\phi^H$     | $\pi_{t-1}$ indexation home good    | 0.5   | 0.15 | <u>0.40</u>    | <u>0.27</u> |
| $\theta^F$   | Calvo prob. foreign good            | 0.75  | 0.1  | 0.87           | 0.86        |
| $\phi^F$     | $\pi_{t-1}$ indexation foreign good | 0.5   | 0.15 | <u>0.46</u>    | <u>0.36</u> |
| $\theta^W$   | Calvo prob wages                    | 0.75  | 0.1  | 0.96           | 0.95        |
| $\phi^W$     | $\pi_{t-1}$ indexation wages        | 0.5   | 0.15 | <u>0.41</u>    | <u>0.67</u> |

- Final good prices: Estimates for Chile indicate a higher probability of periodic price adjustment for home goods, and more indexation to past inflation for both home goods and imported goods.
- Wages: High rigidity is estimated for both countries, albeit more wage indexation to past inflation for Mexico.

# Agenda

- 1 Introduction
- 2 Model and Estimation
  - Selection of Countries
  - Model
  - Parametrization
- 3 Conditional Pass-Through**
  - Shocks Selection
  - Conditional Pass-Through Computation
- 4 Back in VAR
- 5 Conclusions
- 6 Appendices

## Shocks Selection

### Variance Decomposition

|        |         | $v$  | $u$   | $z$   | $a$  | $\zeta$ | $R^*$        | $\pi^*$      | $p^{Co*}$ | $y^{Co}$ | $y^*$ | $g$  | $e_R$       | $\varpi$     |
|--------|---------|------|-------|-------|------|---------|--------------|--------------|-----------|----------|-------|------|-------------|--------------|
| Chile  | $\pi$   | 1.17 | 21.22 | 56.96 | 0.97 | 0.17    | 6.92         | 1.04         | 1.36      | 0.01     | 0.23  | 0.05 | 5.01        | 4.9          |
|        | $\pi^S$ | 0.1  | 1.72  | 0.57  | 0.32 | 1.46    | <u>17.78</u> | <u>29.23</u> | 1.5       | 0.01     | 0.1   | 0    | <u>4.87</u> | <u>42.35</u> |
| Mexico | $\pi$   | 4.5  | 4.51  | 70.86 | 2.82 | 0.4     | 3.04         | 0.01         | 0.59      | 0.01     | 0.32  | 0.01 | 5.73        | 7.2          |
|        | $\pi^S$ | 0.65 | 3.64  | 3.53  | 4    | 3.39    | <u>11.97</u> | 1.89         | 1.69      | 0.02     | 1.79  | 0    | <u>8.65</u> | <u>58.79</u> |

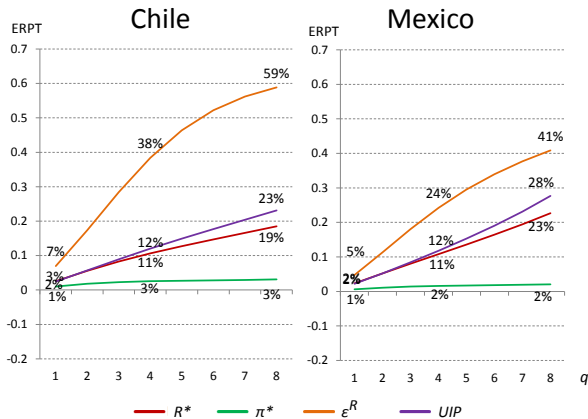
Note: Each column shows the preferences, investment, temporary technology, permanent technology, country premium, international interest rate, international inflation, commodity relative price, commodity production, international aggregate demand, gov. expenditure, monetary policy rate, and UIP deviations shocks.

- UIP shocks, foreign prices shocks, MPR shock and international interest rate shocks together account for 94.2% of variability in the exchange rate in Chile and 81.3% in Mexico.
- Such subset of shocks account for 16/18% of CPI inflation variance.



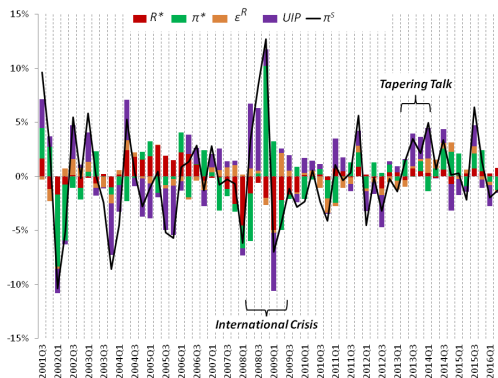
# Conditional ERPT Coefficients

$$ERPT_t^i = \frac{\sum_{j=1}^t IRF_j^{\pi,i}}{\sum_{j=1}^t IRF_j^{\pi^S,i}}$$



# ERPT over time - Chile

## Exchange Rate Historical Variance Decomposition



### Episode

International Crisis

Tapering Talk

### Shock

$\pi^*$

$\epsilon^R$

### Estimated ERPT

$t_1 = 1\%$ ,  $t_4 = 3\%$ ,  $t_8 = 3\%$

$t_1 = 7\%$ ,  $t_4 = 38\%$ ,  $t_8 = 59\%$

# Agenda

- 1 Introduction
- 2 Model and Estimation
  - Selection of Countries
  - Model
  - Parametrization
- 3 Conditional Pass-Through
  - Shocks Selection
  - Conditional Pass-Through Computation
- 4 **Back in VAR**
- 5 Conclusions
- 6 Appendices

## Back in VAR

Tackling Weakness 1: Exchange rate movements assumed exogenous.

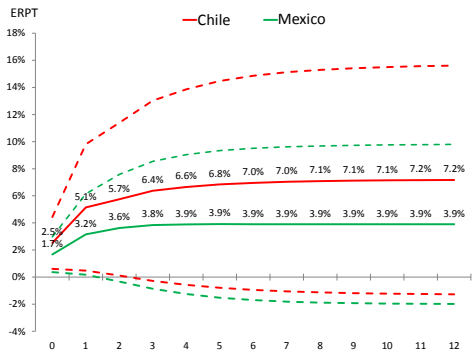
Idea: use simulated data to estimate VAR models.

→ Given that these series are generated using i.i.d shocks, we avoid the aforementioned critique.

- Data:  $n=5000$ ,  $t=70$ .
- Specification: VAR model used in "Selection of Countries" section.

# Back in VAR

## Unconditional ERPT according to VAR model



Note: Dotted lines represent one standard deviation confidence intervals.

Initial VAR estimates showed a 4q pass-through of 8.4% for Chile and of 1.4% for Mexico.

# Agenda

- 1 Introduction
- 2 Model and Estimation
  - Selection of Countries
  - Model
  - Parametrization
- 3 Conditional Pass-Through
  - Shocks Selection
  - Conditional Pass-Through Computation
- 4 Back in VAR
- 5 Conclusions**
- 6 Appendices

# Conclusions

- Goal: Are different ERPT due to different fundamentals or to different distribution of faced shocks?
- Approach:
  - 1) Estimate a DSGE model for two countries with an *a priori* different pass-through.
  - 2) Recover conditional ERPT coefficients.
  - 3) Analyze underlying shocks and compare their distribution.

# Conclusions

- Different conditional coefficients within country.
- Similar conditional coefficients across countries, except that of monetary policy rate.
- Non homogeneous historical variance decomposition: different inflationary consequences would be expected after different episodes.
- Simulated data exercise highlight the importance of shocks accounting for cross-section comparisons.
- Policy implications: Policy response need to be shock conditional.

—→ Evidence suggest that **differences founded in non-conditional estimates are mainly explained by the specific shocks underlying the time series used.**



## Questions and comments

# **Conditional Exchange Rate Pass-Through A DSGE Model Approach**

Mariano J. Palleja

Rodrigo Gómez Award 2018

## A. Review of ERPT Estimates

### Review of ERPT Estimates for Chile

| Reference                          | Period    | Methodology     | ERPT coeff.    |
|------------------------------------|-----------|-----------------|----------------|
| Albagli, Naudon and Vergara (2015) | 2000-2015 | VAR             | 4q: 19%        |
| BBVA (2015)                        | 2000-2015 | VAR             | 4q: 14%        |
| IMF (2016)                         | 2000-2015 | Single Equation | 4q: 6%, 8q:12% |
| Perez-Ruiz (2016)                  | 2003-2015 | VAR             | 4q: 9%, 8q:11% |
| Sansone (2016)                     | 2008-2013 | Partial Eq.     | Cumm.: 9%-20%* |

\*Coefficients depend on elasticities used.

### Review of ERPT Estimates for Mexico

| Reference                                       | Period    | Methodology     | ERPT coeff.  |
|---|-----------|-----------------|--------------|
| Albagli, Naudon and Vergara (2015)              | 2000-2015 | VAR             | 4q: 4%       |
| BBVA (2015)                                     | 2000-2015 | VAR             | 4q: 4%       |
| Capistrán, Ibarra-Ramírez, Ramos-Francia (2012) | 2001-2010 | VAR             | 4q: No sign. |
| Cortés-Espada (2013)                            | 2001-2012 | VAR             | 4q: No sign. |
| Lopez-Villavicencio and Mignon (2016)           | 1994-2015 | Single Equation | 1q: 1.3%     |
| Peón and Rodríguez Brindis (2014)               | 2001-2013 | VAR             | Cumm.: 2.2%  |

## B. Calibrated Parameters - Chile

| Parameter            | Description                              | Value                   | Source                              |
|----------------------|--|-------------------------|-------------------------------------|
| $\omega$             | Share of foreign good in final good      | 0.37                    | M/(C+I+G), 2001q3-2016q2 average    |
| $\alpha$             | Capital share in production              | 0.33                    | Medina and Soto (2007)              |
| $\epsilon_H$         | E.o.S.in aggregate home good             | 11                      | Medina and Soto (2007)              |
| $\chi$               | Government share in commodity production | 0.55                    | $c+(1-c)*t$ , $c=CODELCO/Tot=0.31$  |
| $\delta$             | Capital depreciation                     | 0.015                   | Medina and Soto (2007)              |
| $\epsilon_F$         | E.o.S.in aggregate foreign good          | 11                      | Medina and Soto (2007)              |
| $\epsilon_W$         | E.o.S.in labor demand                    | 11                      | Medina and Soto (2007)              |
| $\rho^{R^*}$         | Auto Corr. $R^*$                         | 0.966                   | AR(1) coeff. sample period          |
| $\rho^{\pi^*}$       | Auto Corr. $\pi^*$                       | 0.4411                  | AR(1) coeff. sample period          |
| $\rho^{C_o^*}$       | Auto Corr. $p^{C_o^*}$                   | 0.9275                  | AR(1) coeff. sample period          |
| $\rho^{y^{C_o}}$     | Auto Corr. $y^{C_o}$                     | 0.654                   | AR(1) coeff. sample period          |
| $\rho^{y^*}$         | Auto Corr. $y^*$                         | 0.912                   | AR(1) coeff. sample period          |
| $\rho^{y^g}$         | Auto Corr. $g$                           | 0.664                   | AR(1) coeff. sample period          |
| $\sigma^{R^*}$       | Std. Dev. of shock to $R^*$              | 0.001                   | AR(1) S.E. (2001q3-2016q2)          |
| $\sigma^{\pi^*}$     | Std. Dev. of shock to $\pi^*$            | 0.0117                  | AR(1) S.E. (2001q3-2016q2)          |
| $\sigma^{p^{C_o^*}}$ | Std. Dev. of shock to $p^{C_o^*}$        | 0.1362                  | AR(1) S.E. (2001q3-2016q2)          |
| $\sigma^{y^{C_o}}$   | Std. Dev. of shock to $y^{C_o}$          | 0.032                   | AR(1) S.E. (2001q3-2016q2)          |
| $\sigma^{y^*}$       | Std. Dev. of shock to $y^*$              | 0.008                   | AR(1) S.E. (2001q3-2016q2)          |
| $\sigma^{y^g}$       | Std. Dev. of shock to $g$                | 0.014                   | AR(1) S.E. (2001q3-2016q2)          |
| $\xi$                | Country Premium in SS                    | 1.0145 <sup>0.25</sup>  | EMBI+Chile, 2001q3-2016q2 average   |
| $a$                  | Long run growth                          | 1.02538 <sup>0.25</sup> | y.o.y GDP pc chg, 2001q3-2016q2 avg |
| $R$                  | Monetary policy rate in SS               | 1.0394 <sup>0.25</sup>  | MP rate, 2001q3-2016q2 avg.         |
| $\pi$                | Inflation in SS                          | 1.03 <sup>0.25</sup>    | Inflation target                    |
| $R^*$                | International interest rate in SS        | 1.0173 <sup>0.25</sup>  | LIBOR rate, 2001q3-2016q2 average   |
| $S^{TB}$             | Trade balance to GDP in SS               | 0.042                   | (X-M)/GDP, 2001q3-2016q2 avg.       |
| $S^G$                | Government exp. to GDP in SS             | 0.117                   | G/GDP, 2001q3-2016q2 avg.           |
| $S^{y^{C_o}}$        | Commodity prod. to GDP in SS             | 0.134                   | Copper prod./GDP, 2001q3-2016q2     |

## B. Calibrated Parameters - Mexico

| Parameter           | Description                              | Value                  | Source                               |
|---------------------|--|------------------------|--------------------------------------|
| $\omega$            | Share of foreign good in final good      | 0.3                    | M/(C+IG), 2003q1-2016q2 average      |
| $\alpha$            | Capital share in production              | 0.34                   | García-Verdú (2005)                  |
| $\epsilon_H$        | E.o.S.in aggregate home good             | 11                     | Adame, Roldan-Peña, Zerecero (2013)  |
| $\chi$              | Government share in commodity production | 1                      | PEMEX                                |
| $\delta$            | Capital depreciation                     | 0.02                   | Adame, Roldan-Peña, Zerecero (2013)  |
| $\epsilon_F$        | E.o.S.in aggregate foreign good          | 11                     | Adame, Roldan-Peña, Zerecero (2013)  |
| $\epsilon_W$        | E.o.S.in labor demand                    | 11                     | Adame, Roldan-Peña, Zerecero (2013)  |
| $\rho^{R^*}$        | Auto Corr. $R^*$                         | 0.979                  | AR(1) coeff. sample period           |
| $\rho^{\pi^*}$      | Auto Corr. $\pi^*$                       | 0.377                  | AR(1) coeff. sample period           |
| $\rho^{p^{Co^*}}$   | Auto Corr. $p^{Co^*}$                    | 0.881                  | AR(1) coeff. sample period           |
| $\rho^{y^{Co}}$     | Auto Corr. $y^{Co}$                      | 0.887                  | AR(1) coeff. sample period           |
| $\rho^{y^*}$        | Auto Corr. $y^*$                         | 0.884                  | AR(1) coeff. sample period           |
| $\rho^{y^g}$        | Auto Corr. $g$                           | 0.612                  | AR(1) coeff. sample period           |
| $\sigma^{R^*}$      | Std. Dev. of shock to $R^*$              | 0.001                  | AR(1) S.E. (2003q1-2016q2)           |
| $\sigma^{\pi^*}$    | Std. Dev. of shock to $\pi^*$            | 0.003                  | AR(1) S.E. (2003q1-2016q2)           |
| $\sigma^{p^{Co^*}}$ | Std. Dev. of shock to $p^{Co^*}$         | 0.168                  | AR(1) S.E. (2003q1-2016q2)           |
| $\sigma^{y^{Co}}$   | Std. Dev. of shock to $y^{Co}$           | 0.016                  | AR(1) S.E. (2003q1-2016q2)           |
| $\sigma^{y^*}$      | Std. Dev. of shock to $y^*$              | 0.006                  | AR(1) S.E. (2003q1-2016q2)           |
| $\sigma^{y^g}$      | Std. Dev. of shock to $g$                | 0.008                  | AR(1) S.E. (2003q1-2016q2)           |
| $\xi$               | Country Premium in SS                    | 1.0204 <sup>0.25</sup> | EMBI+Mexico, 2003q1-2016q2 average   |
| $a$                 | Long run growth                          | 1.0048 <sup>0.25</sup> | y.o.y GDP pc chg, 2003q1-2016q2 avg. |
| $R$                 | Monetary policy rate in SS               | 1.0606 <sup>0.25</sup> | MP rate, 2003q1-2016q2 avg.          |
| $\pi$               | Inflation in SS                          | 1.03 <sup>0.25</sup>   | Inflation Target                     |
| $R^*$               | International interest rate in SS        | 1.017 <sup>0.25</sup>  | LIBOR rate, 2003q1-2016q2 average    |
| $S^{TB}$            | Trade Balance to GDP in SS               | 0.001                  | (X-M)/ GDP, 2003q1-2016q2 avg.       |
| $S^G$               | Government exp. to GDP in SS             | 0.111                  | G/GDP, 2003q1-2016q2 avg.            |
| $S^{y^{Co}}$        | Commodity prod. to GDP in SS             | 0.011                  | PEMEX TB/GDP, 2003q1-2016q2 avg.     |

## C. Variables' Sources and Treatment - Chile

| Variable              | Source                             | Original Variable   | Treatment  |
|-----------------------|------------------------------------|---|--|
| Investment Growth     | Central Bank of Chile              | Gross Fixed Capital Formation (billions of chained pesos), seasonally adjusted, quarterly                   | 1) PC, 2) Log-Diff, 3) DM  |
| Consumption Growth    | Central Bank of Chile              | Private Consumption, millions of pesos at 2008 prices, quarterly  | 1) PC, 2) S.A., 3) Log-Diff, 4) DM   |
| Government Exp.       | Central Bank of Chile              | Government Consumption, millions of pesos at 2008 prices, quarterly   | 1) PC, 2) S.A., 3) Ln, 4) DT, DM   |
| GDP Growth            | Central Bank of Chile              | GDP, millions of chained pesos, seasonally adjusted, quarterly  | 1) PC, 2) Log-Diff, 3) DM  |
| Inflation             | Central Bank of Chile              | CPI General Index, monthly  | 1) Q.A., 2) S.A., 3) Log-Diff, 4) DM   |
| Wage Growth           | INE                                | Remunerations General Index, real, monthly  | 1) Q.A., 2) S.A., 3) Log-Diff, 4) DM   |
| Commodity Prod.       | Central Bank of Chile              | Copper mining, chained volume at previous year prices, seasonally adjusted, quarterly                       | 1) Ln, 2) DT, DM   |
| Commodity Price       | Central Bank of Chile              | Copper price (USD per pound, LME)   | 1) Q.A., 2) Deflated by $\pi^*$ , 3) Ln, 4) DM   |
| Monetary Policy Rat   | Central Bank of Chile              | Monetary Policy Reference Rate, monthly average   | 1) Q.A., 2) Q.R., 3) Ln, 4) DM   |
| Country Premium       | Central Bank of Chile              | Spread - EMBI Chile, monthly average, basis points  | 1) Q.A., 2) Q.R., 3) Ln, 4) DM   |
| NEER Depreciation     | Central Bank of Chile              | Multilateral Exchange Rate, monthly average   | 1) Q.A., 2) Log-Diff, 3) DM  |
| Foreign Interest Rate | St. Louis FRED                     | LIBOR Rate, monthly average.  | 1) Q.A., 2) Q.R., 3) Ln, 4) DM   |
| Foreign GDP           | IMF -IFS and Central Bank of Chile | Trading Partners real GDP (IFS), REER weights (Banco Central Chile), annual                                 | 1) Trading partners real GDP growth weighted by non copper trade flow, 2) S.A., 3) Ln, 4) DT, DM |
| Foreign Inflation     | Central Bank of Chile              | External Prices Index (EPI), Observed dollar (pesos/dollar) (OD), Multilateral exchange rate (MER), monthly | 1) EPI*OD/MER, 2) Q.A., 3) Log-Diff, 4) DM   |
| Population            | U.S. Census Bureau                 | Population older than 16 years, annual.   | Expressed on quarterly basis via linear expansion  |

*Note: PC=per capita, S.A.= X12 seasonally adjusted, Q.A.= quarterly average, Q.R.= Rate expressed on quarterly basis, Ln= natural logarithm, Log-Diff= logarithmic difference between the variable and its one-period lag, DM= deviation from mean, DT= deviation from trend.*

## C. Variables' Sources and Treatment - Mexico

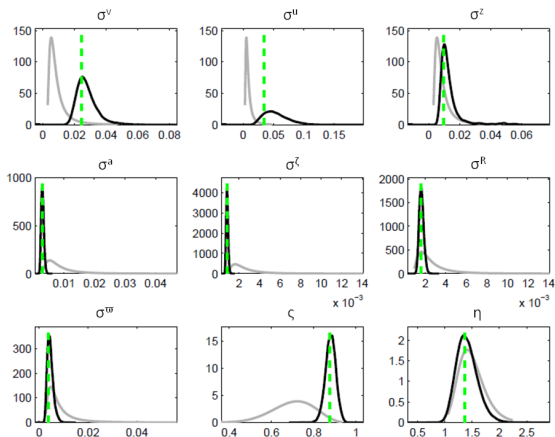
| Variable              | Source  | Original Variable   | Treatment  |
|-----------------------|---|---|--|
| Investment Growth     | INEGI   | Gross Fixed Capital Formation, millions of pesos at 2008 prices, seasonally adjusted, quarterly   | 1) PC, 2) Log-Diff, 3) DM  |
| Consumption Growth    | INEGI   | Private Consumption, millions of pesos at 2008 prices, seasonally adjusted, quarterly   | 1) PC, 2) Log-Diff, 3) DM  |
| Government Exp.       | INEGI   | Government Consumption, millions of pesos at 2008 prices, seasonally adjusted, quarterly  | 1) PC, 2) Ln, 3) DT, DM  |
| GDP                   | INEGI   | GDP, millions of pesos at 2008 prices, seasonally adjusted, quarterly   | 1) PC, 2) Log-Diff, 3) DM  |
| Inflation             | Central Bank of Mexico                        | CPI General Index, monthly  | 1) Q.A., 2) S.A., 3) Log-Diff, 4) DM   |
| Wage Growth           | INEGI, Central Bank of Mexico, St. Louis FRED | Manufacturing industry remuneration in USD per hour (W), monthly. Exchange rate peso/dollar (ER), monthly. CPI General Index ( $\pi$ ), monthly | 1) W*ER/ $\pi$ , 2) Q.A., 3) S.A., 4) Log-Diff, 5) DM  |
| Commodity Prod.       | INEGI   | Liquid Hydrocarbons Production, Raw Oil, thousand barrels per day, monthly  | 1) Q.A., 2) Ln, 3) DT, DM  |
| Commodity Price       | St. Louis FRED                                | Crude Oil Prices: West Texas Intermediate (WTI) - Cushing, Oklahoma, dollars per barrel, monthly  | 1) Q.A., 2) Deflated by $\pi^*$ , 3) Ln, 4) DM   |
| Monetary Policy Rate  | Central Bank of Mexico                        | Interbank Equilibrium Interest Rate (TIIE), at 91 days, annual rate, monthly  | 1) Q.A., 2) Q.R., 3) Ln, 4) DM   |
| Country Premium       | Central Bank of Peru                          | Spread - EMBIG Mexico (basis points), daily   | 1) Q.A., 2) Q.R., 3) Ln, 4) DM   |
| NEER Depreciation     | Central Bank of Mexico                        | World, Currency per U.S. Dollar Index (E*), Pesos per U.S. Dollar Index (E), monthly  | 1) E/E*, 2) Q.A., 3) Log-Diff, 4) DM   |
| Foreign Interest Rate | St. Louis FRED                                | LIBOR Rate, monthly average.  | 1) Q.A., 2) Q.R., 3) Ln, 4) DM   |
| Foreign GDP           | INEGI, IMF-IFS                                | Trading Partners real GDP (IFS), Non Oil Exports and Non Oil Imports (INEGI), quarterly   | 1) Trading partners real GDP growth weighted by non oil trade flow (51 countries), 2) S.A., 3) Ln, 4) DT, DM |
| Foreign Inflation     | Central Bank of Mexico                        | External Price Index (111 countries), monthly   | 1) Q.A., 2) S.A., 3) Log-Diff, 4) DM   |
| Population            | U.S. Census Bureau                            | Population older than 16 years, annual.   | Expressed on quarterly basis via linear expansion  |

Note: PC=per capita, S.A.= X12 seasonally adjusted, Q.A.= quarterly average, Q.R.= Rate expressed on quarterly basis, Ln= natural logarithm, Log-Diff= logarithmic difference between the variable and its one-period lag, DM= deviation from mean, DT= deviation from trend.

# D. Estimated Parameters

| Parameter    | Description                                | Distribution | Prior |          | Posterior Mean |        |
|--------------|--|--------------|-------|----------|----------------|--------|
|              |  |              | Mean  | S.E.     | Chile          | Mexico |
| $\varsigma$  | Consumption habits                         | beta         | 0.7   | 0.1      | 0.88           | 0.567  |
| $\eta$       | E.o.S. between $x_t^H$ and $x_t^F$         | inv gamma    | 1.5   | 0.25     | 1.405          | 1.307  |
| $\eta^*$     | Demand elasticity for exports              | inv gamma    | 0.5   | 0.3      | 0.243          | 0.197  |
| $\alpha^\pi$ | Inflation weight in MPR                    | normal       | 1.5   | 0.1      | 1.494          | 1.549  |
| $\alpha^y$   | Product weight in MPR                      | normal       | 0.13  | 0.05     | 0.145          | 0.148  |
| $\rho^R$     | $R_{t-1}$ weight in MPR                    | beta         | 0.75  | 0.1      | 0.84           | 0.8    |
| $\psi$       | Country premium elasticity                 | inv gamma    | 0.01  | 0.013    | 0.007          | 0.004  |
| $\gamma$     | Investment adjustment costs                | normal       | 4     | 1.5      | 3.019          | 2.911  |
| $\theta^H$   | Calvo prob. home goods                     | beta         | 0.75  | 0.1      | 0.501          | 0.722  |
| $\phi^H$     | Indexation to $\pi_{t-1}$ in home goods    | beta         | 0.5   | 0.15     | 0.396          | 0.267  |
| $\theta^F$   | Calvo prob. foreign goods                  | beta         | 0.75  | 0.1      | 0.874          | 0.865  |
| $\phi^F$     | Indexation to $\pi_{t-1}$ in foreign goods | beta         | 0.5   | 0.15     | 0.457          | 0.36   |
| $\theta^W$   | Calvo prob. wages                          | beta         | 0.75  | 0.1      | 0.963          | 0.953  |
| $\phi^W$     | Indexation to $\pi_{t-1}$ in wages         | beta         | 0.5   | 0.15     | 0.411          | 0.672  |
| $\rho^v$     | Auto Corr. preferences shock               | beta         | 0.75  | 0.1      | 0.867          | 0.692  |
| $\rho^u$     | Auto Corr. investment shock                | beta         | 0.75  | 0.1      | 0.703          | 0.716  |
| $\rho^z$     | Auto Corr. temp. tecn. shock               | beta         | 0.75  | 0.1      | 0.762          | 0.568  |
| $\rho^a$     | Auto Corr. perm. tecn. shock               | beta         | 0.38  | 0.1      | 0.344          | 0.197  |
| $\rho^c$     | Auto Corr. country premium shock           | beta         | 0.75  | 0.1      | 0.83           | 0.859  |
| $\rho^w$     | Auto Corr. UIP shock                       | beta         | 0.75  | 0.1      | 0.829          | 0.864  |
| $\sigma^v$   | Std. Dev. preferences shock                | inv gamma    | 0.01  | 0.013    | 0.028          | 0.025  |
| $\sigma^u$   | Std. Dev. investment shock                 | inv gamma    | 0.01  | 0.013    | 0.053          | 0.021  |
| $\sigma^z$   | Std. Dev. temp. tecn. shock                | inv gamma    | 0.01  | 0.013    | 0.013          | 0.029  |
| $\sigma^a$   | Std. Dev. perm. tecn. shock                | inv gamma    | 0.01  | 0.013    | 0.003          | 0.008  |
| $\sigma^c$   | Std. Dev. country premium shock            | inv gamma    | 0.003 | 0.004    | 0.001          | 0.001  |
| $\sigma^R$   | Std. Dev. MPR shock                        | inv gamma    | 0.003 | 0.004    | 0.002          | 0.002  |
| $\sigma^w$   | Std. Dev. UIP shock                        | inv gamma    | 0.01  | $\infty$ | 0.005          | 0.004  |

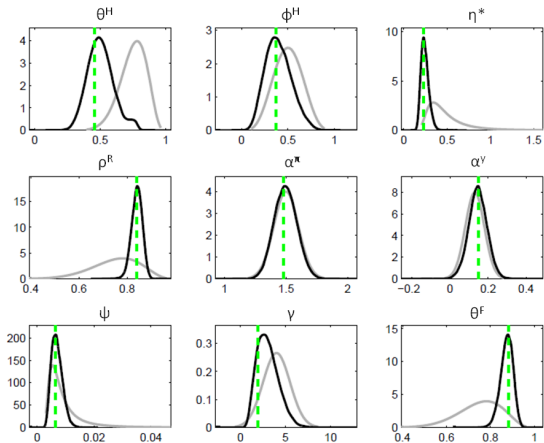
## E. Priors and Posteriors - Chile



Note: Horizontal and vertical axis represent the prior range distribution and the cumulative density, respectively. The grey, black and green lines indicate the prior density, posterior density, and posterior mode, respectively.

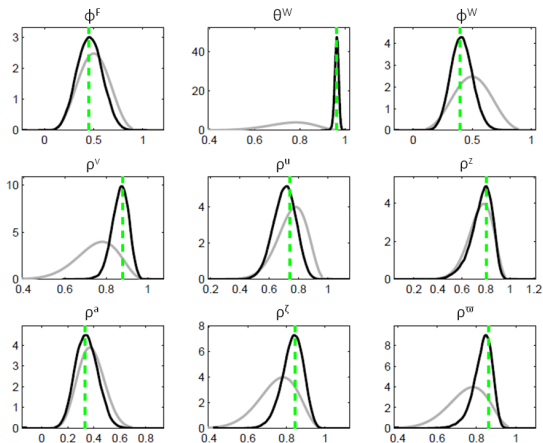


## E. Priors and Posteriors - Chile



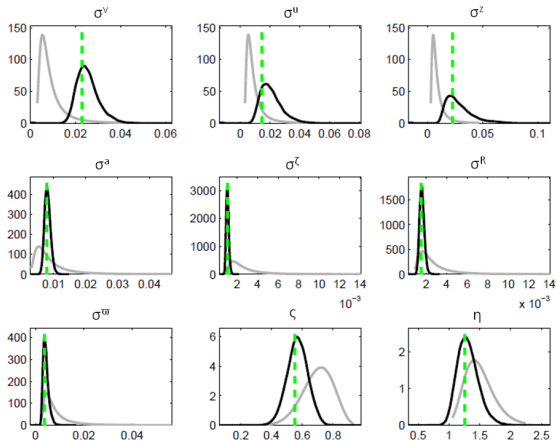
Note: Horizontal and vertical axis represent the prior range distribution and the cumulative density, respectively. The grey, black and green lines indicate the prior density, posterior density, and posterior mode, respectively.

## E. Priors and Posteriors - Chile



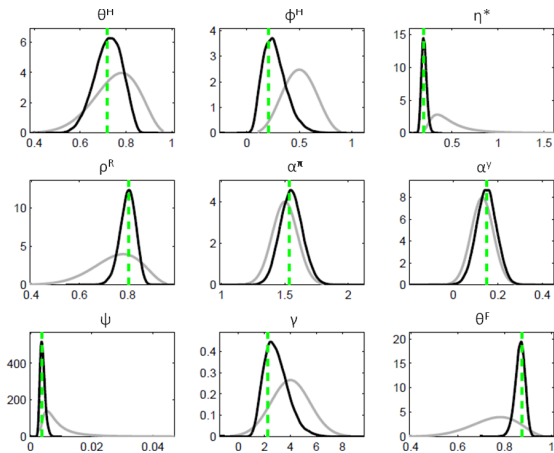
Note: Horizontal and vertical axis represent the prior range distribution and the cumulative density, respectively. The grey, black and green lines indicate the prior density, posterior density, and posterior mode, respectively.

## E. Priors and Posteriors - Mexico



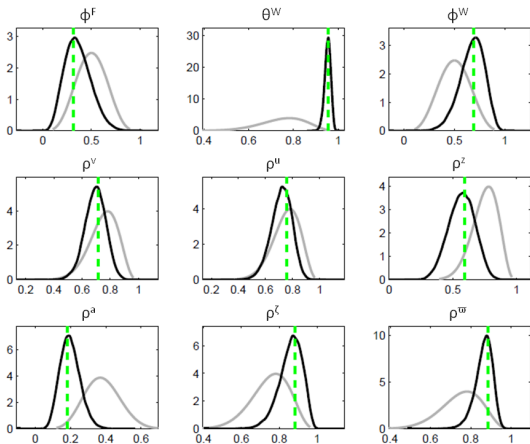
Note: Horizontal and vertical axis represent the prior range distribution and the cumulative density, respectively. The grey, black and green lines indicate the prior density, posterior density, and posterior mode, respectively.

## E. Priors and Posteriors - Mexico



Note: Horizontal and vertical axis represent the prior range distribution and the cumulative density, respectively. The grey, black and green lines indicate the prior density, posterior density, and posterior mode, respectively.

## E. Priors and Posteriors - Mexico



Note: Horizontal and vertical axis represent the prior range distribution and the cumulative density, respectively. The grey, black and green lines indicate the prior density, posterior density, and posterior mode, respectively.

## F. Estimation Fit

### Selected Second Order Moments

|                    |           | Chile |       |                  |      | Mexico |       |                  |       |
|--------------------|-----------|-------|-------|------------------|------|--------|-------|------------------|-------|
|                    |           | S.E.  |       | Autocorr. Coeff. |      | S.E.   |       | Autocorr. Coeff. |       |
|                    |           | Model | Data  | Model            | Data | Model  | Data  | Model            | Data  |
| MPR                | $R$       | 0.55  | 0.41  | 0.92             | 0.88 | 0.44   | 0.48  | 0.88             | 0.95  |
| Country Premium    | $\xi$     | 0.26  | 0.15  | 0.93             | 0.83 | 0.54   | 0.17  | 0.97             | 0.78  |
| Inflation          | $\pi$     | 0.69  | 0.70  | 0.67             | 0.57 | 0.55   | 0.33  | 0.62             | 0.08  |
| International Rate | $R^*$     | 0.39  | 0.43  | 0.97             | 0.97 | 0.48   | 0.44  | 0.98             | 0.98  |
| Foreign Inflation  | $\pi^*$   | 1.30  | 1.30  | 0.44             | 0.44 | 0.37   | 0.37  | 0.38             | 0.38  |
| Commodity Rel. P   | $p^{C0*}$ | 36.43 | 45.44 | 0.93             | 0.95 | 35.37  | 35.14 | 0.88             | 0.88  |
| Commodity Prod.    | $Y^{Co}$  | 4.22  | 4.27  | 0.65             | 0.66 | 3.56   | 3.83  | 0.89             | 0.9   |
| Foreign GDP        | $Y^*$     | 1.98  | 1.45  | 0.91             | 0.83 | 1.27   | 1.49  | 0.88             | 0.91  |
| Gov. Expenditure   | $G$       | 1.89  | 1.92  | 0.66             | 0.67 | 1.01   | 0.99  | 0.61             | 0.61  |
| NEER Depreciation  | $\pi^S$   | 4.93  | 4.27  | -0.04            | 0.15 | 4.51   | 4.37  | -0.05            | 0.04  |
| GDP Growth         | $g^Y$     | 1.12  | 1.04  | 0.33             | 0.19 | 0.94   | 0.97  | 0.43             | 0.47  |
| C Growth           | $g^C$     | 0.60  | 0.75  | 0.79             | 0.93 | 1.25   | 1.30  | 0.37             | 0.44  |
| I Growth           | $g^I$     | 4.60  | 4.03  | 0.62             | 0.21 | 2.47   | 1.82  | 0.72             | 0.51  |
| W Growth           | $g^G$     | 0.61  | 0.6   | 0.39             | 0.31 | 0.89   | 0.99  | 0.18             | -0.40 |

Note: Unconditional moments computed at the posterior mean. Standard deviations are presented as percentage points.

## G. Model Dynamics

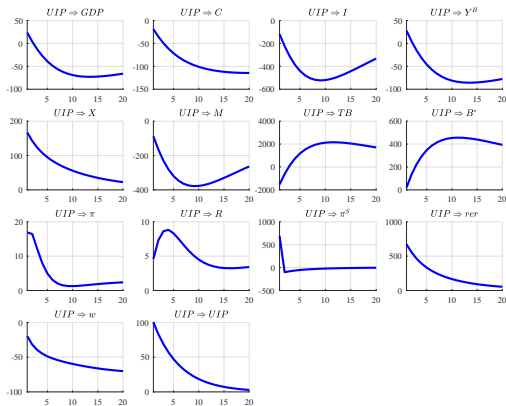
*UIP* shock:

- Exchange rate depreciates
  - Real exchange rate depreciates, which rises the price of both imports and exports.
  - Positive effect over GDP.  
→ Positive effect over inflation.
- Internal and external financing cost rise.
  - Negative income effect (net debt) and negative substitution effect (present consumption and investment are translated to the future), both implying negative effect over GDP.  
→ Negative effect over inflation.

The first effect dominates, hence we have a positive ERPT.

# G. Model Dynamics

## *UIP* shock - Impulse Response Function



The shock was normalized to represent a 1 p.p. deviation, and responses of the variables are expressed in percentage deviations (basis points) in relation to their steady state. Impulse-response functions shown herein correspond to the Chilean case; however, the dynamics are similar for Mexico.



## G. Model Dynamics

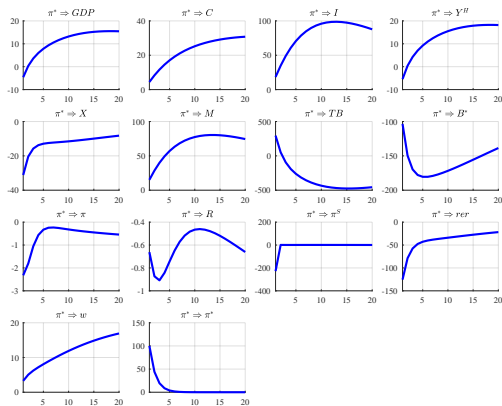
### Foreign price shock

- Incremento en los costos marginales de la industria importadora  
→ Efecto contractivo e impacto positivo sobre la inflación.
- Incremento en la demanda de exportaciones  
→ Efecto expansivo e impacto positivo sobre la inflación.
- Reducción del costo de financiamiento externo y reducción del stock de deuda extranjera.
  - Reducción en el *country premium* y apreciación nominal
$$\widehat{R}_t = \widehat{R}_t^* + \widehat{\xi}_t + \mathbb{E}_t[\widehat{\pi}_{t+1}^S] + \widehat{\omega}_t$$
  
→ Efecto expansivo e impacto negativo sobre la inflación.

En conjunto, el efecto de la apreciación nominal sobre el tipo de cambio real sobrepasa el incremento en precios foráneos. Se reducen los precios y el ERPT es positivo.

# G. Model Dynamics

## Foreign price shock - Impuls Response Function



The shock was normalized to represent a 1 p.p. deviation, and responses of the variables are expressed in percentage deviations (basis points) in relation to their steady state. Impulse-response functions shown herein correspond to the Chilean case; however, the dynamics are similar for Mexico.

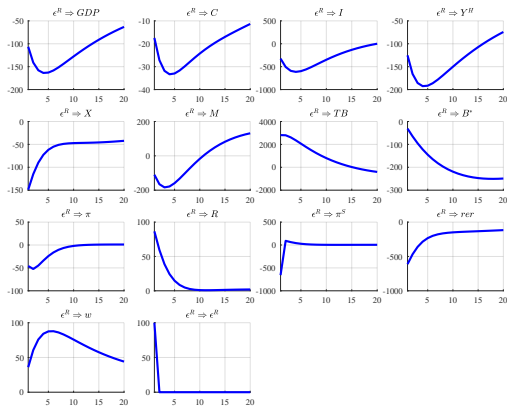
## G. Model Dynamics

### Monetary policy rate shock

- Incremento en el costo de financiamiento interno.
  - Efecto ingreso negativo y traslado de consumo e inversión hacia el futuro, ambos con efectos contractivos.  
→ Impacto negativo sobre la inflación.
- Desbalance de la UIP, lo cual implica una apreciación en el tipo de cambio nominal  
Tipo de cambio y precios en el mismo sentido: ERPT positivo.

# G. Model Dynamics

## Monetary policy rate shock - Impulse Response Function



The shock was normalized to represent a 1 p.p. deviation, and responses of the variables are expressed in percentage deviations (basis points) in relation to their steady state. Impulse-response functions shown herein correspond to the Chilean case; however, the dynamics are similar for Mexico.

## G. Model Dynamics

$R^*$  shock

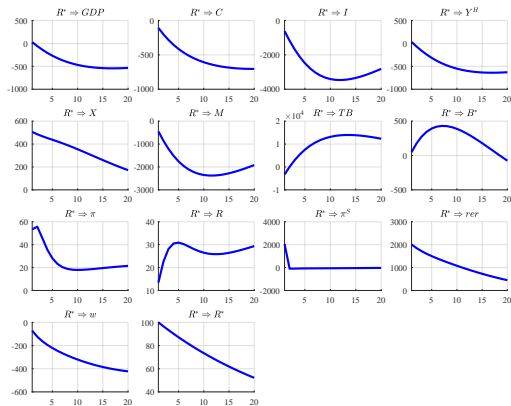
Mismos efectos cualitativos que shock a la *UIP*

- Incremento en el costo de financiamiento.
  - Efecto ingreso negativo (deudor neto) y traslado de consumo e inversión hacia el futuro, ambos con efectos contractivos.  
→ Impacto negativo sobre la inflación.
- Incremento en el tipo de cambio.
  - Incremento del tipo de cambio real, el cual impulsa el precio de las importaciones y de las exportaciones
  - Efecto expansivo sobre el producto  
→ Impacto positivo sobre la inflación.

En conjunto, el segundo efecto prepondera sobre la dinámica de precios: ERPT positivo.

# G. Model Dynamics

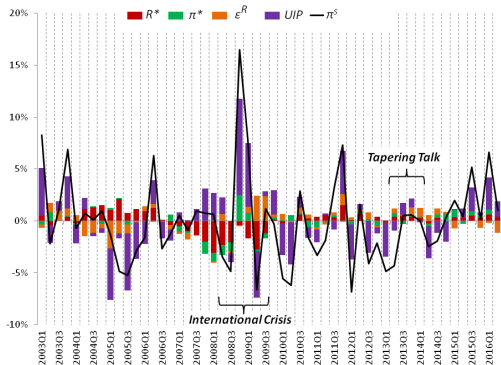
## $R^*$ shock - Impulse Response Function



The shock was normalized to represent a 1 p.p. deviation, and responses of the variables are expressed in percentage deviations (basis points) in relation to their steady state. Impulse-response functions shown herein correspond to the Chilean case; however, the dynamics are similar for Mexico.

# H. ERPT over time - México

## Exchange Rate Historical Variance Decomposition



### Episode

International Crisis

Tapering Talk

### Shock

$\pi^*$

$\epsilon^R$

### Estimated ERPT

$t_1 = 1\%$ ,  $t_4 = 2\%$ ,  $t_8 = 2\%$

$t_1 = 5\%$ ,  $t_4 = 24\%$ ,  $t_8 = 41\%$